Staple Inn Hall, High Holborn, London

A value-at-risk framework for longevity trend risk

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The Actuarial Profession

making financial sense of the future

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1. The need for stochastic projections

"computation of the SCR for longevity risk via the VaR approach obviously requires stochastic modelling of mortality"

Boerger (2010)

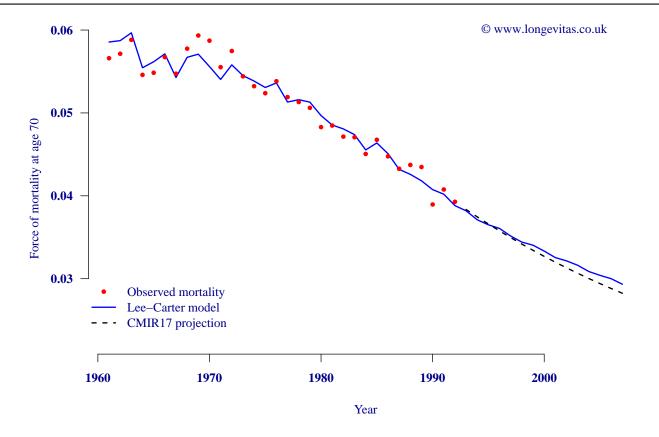
"naturally this requires stochastic mortality rates"

Plat (2011)

An illustration — back-testing

- Take a long data series
- Discard latter years and fit projection model
- Compare projected rates with what actually happened

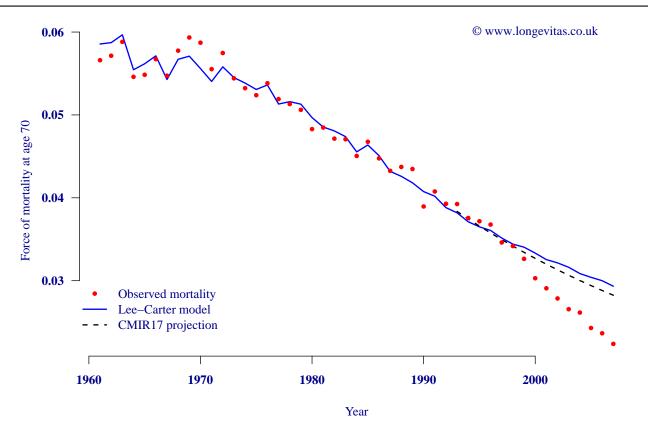
Back-testing: fit model to data to 1992



Source: Longevitas Ltd. ONS data, CMIR17

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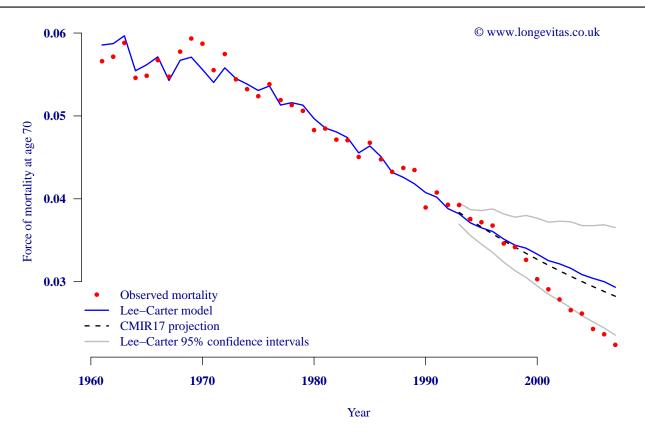
Back-testing: compare projections to actual data



Source: Longevitas Ltd. ONS data, CMIR17

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Back-testing: compare data to confidence intervals

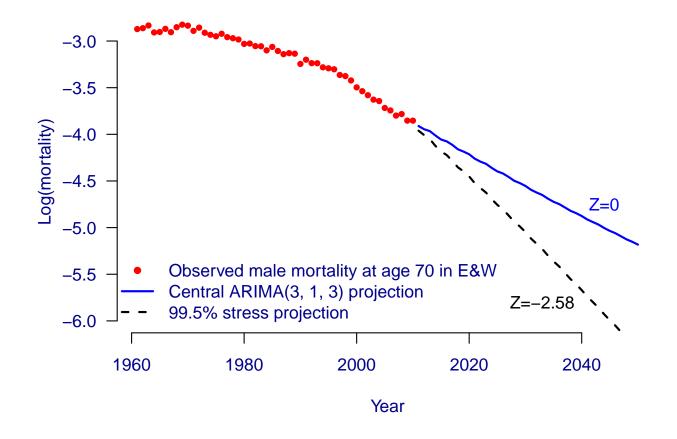


Source: Longevitas Ltd. ONS data, CMIR17

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2. The stressed-trend approach

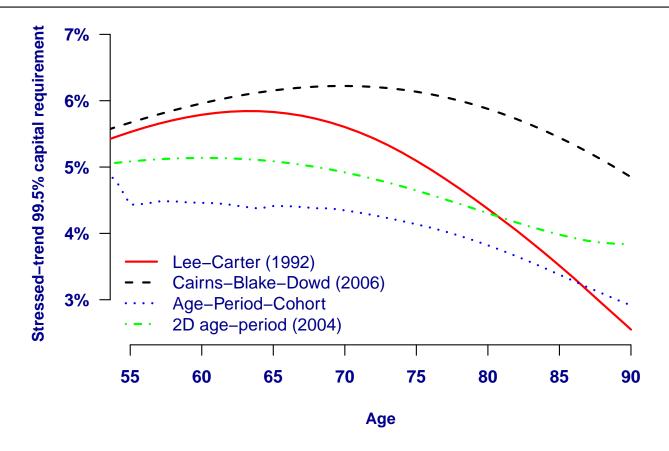
The stressed-trend approach



Source: Richards, Currie and Ritchie (2012), Figure 1.

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The importance of model risk

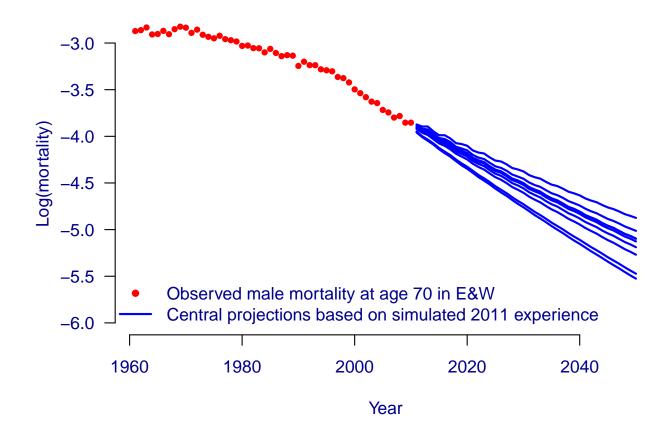


Source: Richards, Currie and Ritchie (2012), Figure 2.

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3. A value-at-risk (VaR) framework

Lee-Carter VaR with 1,000 simulations

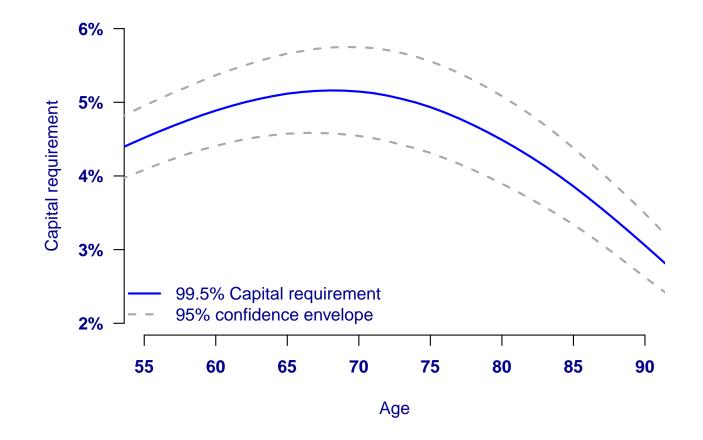


Source: Richards, Currie and Ritchie (2012), Figure 5.

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4. Number of simulations required

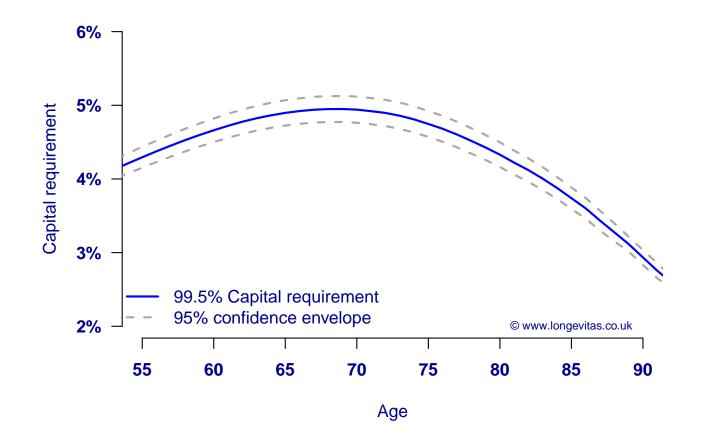
Lee-Carter VaR with 1,000 simulations



Source: Richards, Currie and Ritchie (2012), Figure 6.

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Lee-Carter VaR with 10,000 simulations

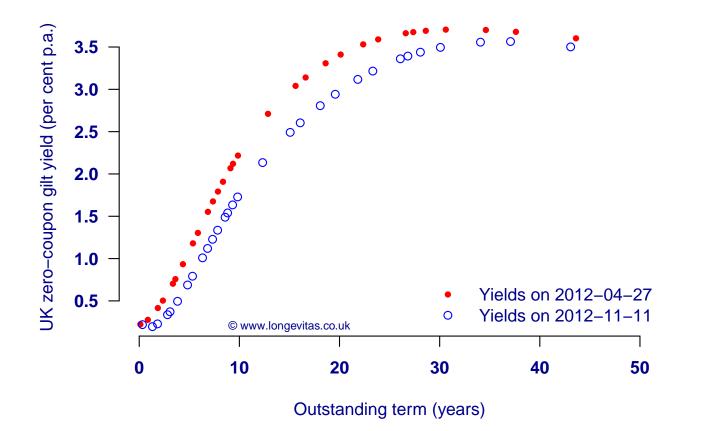


Source: Longevitas Ltd.

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5. The need to regularly recalibrate VaR capital

UK zero-coupon gilt yield curve



Source: Data from Debt Management Office, http://www.dmo.gov.uk

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6. Conclusions

- Deterministic scenarios limited by lack of likelihood
- Stochastic projections needed to include uncertainty
- Stressed-trend approach too strong for one-year view
- Model risk must be acknowledged and different models used
- VaR capital needs to be regularly recalibrated if yield curve changes



References

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LEE, R. D. AND CARTER, L. **1992** Modelling and forecasting the time series of US mortality, Journal of the American Statistical Association **87**, 659–671

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Addendum 1: Parallel VaR — 4 processes

Model	Scalability factor
Lee-Carter Gompertz	$4.0 \mathrm{x}$
CBD5 P-spline	$4.0 \mathrm{x}$
2D Age-cohort	$3.9 \mathrm{x}$
CBD5 Gompertz	$3.8 \mathrm{x}$
Lee-Carter Original	$3.8 \mathrm{x}$
APC Original	$3.7\mathrm{x}$
Lee-Carter Smooth	$3.6 \mathrm{x}$

Source: Longevitas Ltd. The scalability factor is the speed increase relative to serial processing.

Addendum 2: Parallel	VaR - 7 processes
\mathbf{Model}	Scalability factor

Lee-Carter Original	6.6x
Lee-Carter Smooth	6.6x
Lee-Carter Gompertz	6.6x
CBD5 P-spline	$5.8 \mathrm{x}$
2D Age-cohort	$5.1 \mathrm{x}$
APC Original	$5.0 \mathrm{x}$
CBD5 Gompertz	4.1x

Source: Longevitas Ltd. The scalability factor is the speed increase relative to serial processing.